# An X-Ray Powder Diffraction Study of the NdBr<sub>3</sub>–TbCl<sub>3</sub> System

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Received October 25, 1988; in revised form February 6, 1989

The NdBr<sub>3</sub>-TbCl<sub>3</sub> system has been investigated by the Guinier X-ray powder diffraction technique over the full composition range. Four discrete phase regions were identified. Orthorhombic PuBr<sub>3</sub>-type solid solution regions were observed from 0 to  $\sim$ 12.5 and 52.5 to 100 mole% NdBr<sub>3</sub>. A hexagonal UCl<sub>3</sub>-type region was apparent between 5 and  $\sim$ 60 mole% NdBr<sub>3</sub>, and a monoclinic AlCl<sub>3</sub>-type region was found between  $\sim$ 15 and 50 mole% NdBr<sub>3</sub>. Between 7.5 and  $\sim$ 17.5 mole% NdBr<sub>3</sub> a high-temperature phase which could not be characterized was also observed. Phase limits in the 7.5–17.5 mole% region were particularly sensitive to annealing conditions. © 1989 Academic Press, Inc.

#### Introduction

Studies of mixed trihalide systems  $LnX_{3}$ - $Ln'Y_3$ , where Ln and Ln' represent different lanthanoid elements and X and Y are the Cl, Br, or I anions, provide unique opportunities to examine the effects of slight cation and anion size differences on structural properties. Numerous lanthanoid mixedhalide ternary systems have recently been examined by X-ray diffraction and thermal techniques (1-3). Exemplary systems (with the structure types indicated in parentheses) are: LaCl<sub>3</sub>–LaBr<sub>3</sub>  $(UCl_3 - UCl_3),$ NdCl<sub>3</sub>-NdBr<sub>3</sub> (UCl<sub>3</sub>-PuBr<sub>3</sub>), GdCl<sub>3</sub>-DyCl<sub>3</sub> (UCl<sub>3</sub>-AlCl<sub>3</sub>), TbCl<sub>3</sub>-TbBr<sub>3</sub> (PuBr<sub>3</sub>-AlCl<sub>3</sub>), DyCl<sub>3</sub>-HoCl<sub>3</sub> (AlCl<sub>3</sub>-AlCl<sub>3</sub>), and YbCl<sub>3</sub>-YbBr<sub>3</sub> (AlCl<sub>3</sub>-FeCl<sub>3</sub>). Nonisomorphous parent phases usually produce either eutectic structures or two solid solution regions with one or more different structure-type phase also present between these solid solution regions (2-4). Isomorphous systems, on the other hand, typically exhibit only continuous solid solution over the full composition range (1, 2, 4). Isomorphous solid solution behavior has been observed with different-sized cations in the DyCl<sub>3</sub>-HoCl<sub>3</sub> system (2) and with different-sized anions in the LaCl<sub>3</sub>-LaBr<sub>3</sub> system (1).

The quaternary TbCl<sub>3</sub>-NdBr<sub>3</sub> system in which both parent phases exhibit the PuBr<sub>3</sub>type structure is of particular interest. In the TbCl<sub>3</sub>-TbBr<sub>3</sub> system with increasing mole% TbBr<sub>3</sub> a PuBr<sub>3</sub>-type solid solution region, a two-phase region, and an extended AlCl<sub>3</sub>-type solid solution region are found (3). In the NdCl<sub>3</sub>-NdBr<sub>3</sub> system with increasing mole% NdBr<sub>3</sub> an extended UCl<sub>3</sub>type solid solution region, a two-phase region, and a narrow PuBr<sub>3</sub>-type solid solution region prevail (1).

The CN VIII ionic radii of  $Tb^{3+}$  and  $Nd^{3+}$ differ by 0.07 Å; the CN VI radii of Cl<sup>-</sup> and Br<sup>-</sup> differ by 0.15 Å (5). However, the volume mismatch, defined as  $(V_2-V_1)/V_{12}$ ,

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where  $V_{12}$  represents the mean of the two molar volumes, is 0.209 (4). Thus, even though on the basis of parent structure types this NdBr<sub>3</sub>-TbCl<sub>3</sub> system might exhibit continuous solid solution (4), both the limited solubility of bromide ions in TbCl<sub>3</sub> and chloride ions in NdBr<sub>3</sub> (1, 3) and potential changes in the structure caused by the internal pressure which results from the presence of different-sized ions (6) were expected to make the phase relationships complex and unpredictable. Consequently, a systematic study of the title system was undertaken; its results are presented below.

### **Experimental**

The reactants TbCl<sub>3</sub> and NdBr<sub>3</sub> were synthesized, respectively, from Tb<sub>2</sub>O<sub>3</sub> (prepared by hydrogen reduction of "Tb<sub>4</sub>O<sub>7</sub>") and  $Nd_2O_3$  (both 99.9%, from Michigan Chemical Co.). Synthesis was effected according to the ammonium halide matrix procedure (7, 8) with NH<sub>4</sub>Cl (ACS reagent grade, Fisher Scientific) in a 1:6 molar ratio and NH<sub>4</sub>Br (ACS reagent grade, Matheson) in a 1:8 molar ratio as described previously (3). The trihalides were purified by distillation at  $10^{-6}$  Torr (9). All manipulations of reactants and products were effected in a glove box whose Ar atmosphere was continuously purged of H<sub>2</sub>O (molecular sieves) and oxygen (heated BASF catalyst).

The TbCl<sub>3</sub>-NdBr<sub>3</sub> system was studied over the full composition range in steps of 2.5, 5, or 10 mole% depending upon the nature of the results. Mixed trihalide specimens, each of which had a total mass of 0.3 g, were intimately ground in an agate mortar in the desired stoichiometric ratio according to:

$$x \operatorname{TbCl}_{3} + (1 - x) \operatorname{NdBr}_{3} \rightarrow \operatorname{Tb}_{x} \operatorname{Nd}_{(1-x)} \operatorname{Cl}_{3x} \operatorname{Br}_{(3-3x)}.$$
 (1)

After transfer to 7-mm-i.d. previously outgassed quartz tubes the samples were melted with a hand torch under a vacuum of 10<sup>-3</sup> Torr and then quenched to room temperature. Selected specimens (7.5, 10, 17.5, 20, and 52.5 mole% NdBr<sub>3</sub>) were resealed into outgassed quartz tubes, heated in a Thermco Minibrute furnace to 588°C, the TbCl<sub>3</sub> melting point (9), cooled at  $2^{\circ}$ C/hr to 400°C, then left to cool in the oven which was shut off. Two other resealed specimens (10 and 12 mole% NdBr<sub>3</sub>) were heated to 580°C, cooled at 5°C/hr to 320°C, and then at 30°C/hr to room temperature. All products were pulverized in an agate mortar and examined in an evacuated 114.6-mm-diameter Guinier-Hägg X-ray camera with  $CuK\alpha_1$  ( $\lambda\alpha_1 = 1.54050$  Å) radiation and NBS certified Si (a = 5.430825(36) Å) as internal standard. Reflection positions were determined as described previously (3). Lattice parameters were determined initially with a locally written least-squares program and refined subsequently with the program APPLEMAN (10). For selected compositions theoretical X-ray powder reflection intensities were calculated with the program POWD12 (11); calculations were effected on a VAX 11/750.

## Results

Mass balance confirmed that the final composition could be considered identical to the mixed composition. There was no apparent attack of the quartz container during the short interval that the samples were molten. Even specimens that were annealed over a period of 4 days did not attack the quartz container appreciably. Oxidehalide reflections were never observed.

Both TbCl<sub>3</sub> and NdBr<sub>3</sub> reagents crystallized in the PuBr<sub>3</sub>-type (*Cmcm*) structure (12). The observed lattice parameters for these reagents are in good agreement with literature values (13, 14); observed intensities corresponded well to calculated values. Lattice parameters for these parent phases and for the phases present at selected com-

Overall composition	% TbCl <sub>3</sub>	Struct. type	a (Å)	b (Å)	c (Å)	β (°)	Ref. <sup>a</sup>
TbCl <sub>3</sub>	100	PuBr <sub>3</sub>	3.847(2)	11.771(5)	8.516(4)		(12)
			3.846(1)	11.766(5)	8.515(3)		
$Tb_{0.95}Nd_{0.05}Cl_{2.85}Br_{0.15}$	95	PuBr₃	3.857(2)	11.845(5)	8.546(2)		
		(UCl <sub>3</sub> <sup>b</sup>	7.403(1)		4.112(1)		
0.9(TbCl <sub>3</sub> ) · 0.1(NdBr <sub>3</sub> )	90	{ UCl <sub>3</sub> <sup>c</sup>	7.410(4)		4.132(6)		
		PuBr <sub>3</sub> <sup>c</sup>	3.85(1)	11.86(2)	8.58(1)		
0.8(TbCl <sub>3</sub> ) · 0.2(NdBr <sub>3</sub> )	80	`UCl₃	7.448(1)		4.158(2)		
		AlCl <sub>3</sub>	7.031(2)	12.177(1)	6.58(1)	110.74(1)	
$0.7(\text{TbCl}_3) \cdot 0.3(\text{NdBr}_3)$	70	UCI3	7.503(9)		4.194(1)		
		AlCl <sub>3</sub>	7.048(5)	12.209(7)	6.577(1)	110.93(1)	
$0.6(TbCl_3) \cdot 0.4(NdBr_3)$	60	UCl <sub>3</sub>	7.562(2)		4.221(4)		
		AlCl <sub>3</sub>	7.095(4)	12.282(5)	6.633(4)	110.69(1)	
$0.5(TbCl_3) \cdot 0.5(NdBr_3)$	50	UCl₃	7.623(2)		4.259(3)		
		AlCl <sub>3</sub>	7.124(3)	12.343(4)	6.687(3)	110.96(1)	
0.47(TbCl <sub>3</sub> ) · 0.53(NdBr <sub>3</sub> )	47	UCl <sub>3</sub>	7.637(1)		4.264(1)		
Tb <sub>0.35</sub> Nd <sub>0.65</sub> Cl <sub>1.05</sub> Br <sub>1.95</sub>	35	PuBr <sub>3</sub>	4.040(1)	12.501(4)	9.001(2)		
NdBr <sub>3</sub>	0	PuBr <sub>3</sub>	4.108(6)	12.637(9)	9.141(7)		
		-	4.10(3)	12.63(5)	9.15(4)		(13)

TABLE I

LATTICE PARAMETER DATA FOR SELECTED COMPOSITIONS IN THE NdBr3-TbCl3 SYSTEM

<sup>a</sup> This work, except as noted.

<sup>b</sup> Quenched.

<sup>c</sup> Annealed.

positions are presented in Table I. Phase relationships in the mixed-halide system are presented schematically in Fig. 1. In this system orthorhombic PuBr<sub>3</sub>-type solid solution regions extend from 0 to  $\sim 12.5$  and

from 52.5 to 100 mole% NdBr<sub>3</sub>. A hexagonal UCl<sub>3</sub>-type region is found between 5 and ~60 mole% NdBr<sub>3</sub>, and a monoclinic AlCl<sub>3</sub>type region spans ~15 to 50 mole% NdBr<sub>3</sub>. Between 7.5 and ~17.5 mole% NdBr<sub>3</sub> two



FIG. 1. A schematic representation of the TbCl<sub>3</sub>-NdBr<sub>3</sub> system as a function of composition. The blocks represent the composition range over which the designated phase is observed in the X-ray diffraction pattern. The letter H represents a quenchable high-temperature modification. Diphasic regions span  $5-\sim12.5$ ,  $\sim15-50$ , and  $52.5-\sim60$  mole% NdBr<sub>3</sub>.

interplanar composition dependent *d*-spacings (with intensities), 5.464 (vvw) and 4.667 Å (m), which could not be assigned to any expected phase were observed consistently along with the PuBr<sub>3</sub>- and UCl<sub>3</sub>-type reflections in the quenched specimens. The annealed 7.5, 10, and 12.5 mole% NdBr<sub>3</sub> specimens, on the other hand, did not evidence these reflections.

The various diphasic regions, expressed in terms of mole% NdBr<sub>3</sub>, and the structure types observed in them are: 5 to ~12.5, PuBr<sub>3</sub>- and UCl<sub>3</sub>-types; ~15 to 50, UCl<sub>3</sub>and AlCl<sub>3</sub>-types; and 52.5 to ~60, UCl<sub>3</sub>and PuBr<sub>3</sub>-types. Monophasic regions, expressed in terms of mole% NdBr<sub>3</sub>, span 0 to 5, PuBr<sub>3</sub>-type; ~12.5 to 15 and 50 to 52.5, UCl<sub>3</sub>-type; and 60 to 100, PuBr<sub>3</sub>-type.

## Discussion

Assignment of X-ray reflections to the PuBr<sub>3</sub>- and UCl<sub>3</sub>-type structures was straightforward. The UCl<sub>3</sub>-type reflections corresponded very closely to those in the UCl<sub>3</sub>-type region of the Gd-Cl-Br system, and assignment could be made visually by comparing adjacently situated Guinier diffraction films. Assignment of the remaining reflections to the AlCl<sub>3</sub>-type structure, on the other hand, was tenuous and difficult. In both the Gd-Cl-Br and Tb-Cl-Br systems this monoclinic structure was characterized by broad, weak reflections. After UCl<sub>3</sub>-type reflections had been assigned in this quaternary system, typically only eight broad frequently weak reflections remained, and these in addition to potential superpositions based upon intensity considerations constituted the evidence for the monoclinic phase. However, the accuracy of this assignment is enhanced by X-ray powder intensity calculations which indicate that for the AlCl<sub>3</sub> phase the first reflection should be the most intense (11). It should be followed first by weaker reflections, and then by very weak reflections. This pattern of intensity variation was observed for the 15-50 mole% NdBr<sub>3</sub> specimens.

The two extra X-ray reflections apparent in the 7.5-~17.5 mole% NdBr3 region could not be assigned definitively to the FeCl<sub>3</sub>- or the high-pressuure RhF<sub>3</sub>- or PuBr<sub>3</sub>-type structures common to species with these radius ratios (15-17). Nor could they be assigned to oxide or oxidehalide phases or to known hydrate phases. (Hydrate phases were not expected since the moisture level in the glove box was typically 3.5 ppm<sub>v</sub>, as recorded on an ONDYNE moisture content monitor when experiments were being repeated.) The inability to assign these two reflections to any known phase, their variation with composition, and the fact that annealed specimens do not exhibit them suggest strongly that they result from a quenched high-temperature modification. The phase can only be characterized by increasing its concentration, probably through either high-temperature X-ray or high-pressure experiments, or through more rapid quenching.

The region 7.5-17.5 mole% NdBr<sub>3</sub> was difficult to interpret as the results depend upon annealing conditions. For example, in the 5°C/hr annealed 10 mole% specimen the moderately intense 5.464 and 4.667 Å reflections were absent, but three very weak (7.785, 7.181, 3.952 Å) and one weak (3.1696 Å) reflection in addition to clearly indexable UCl<sub>3</sub>- and PuBr<sub>3</sub>-type reflections were present. The quenched 10 and 12 mole% specimens did not evidence any PuBr<sub>3</sub>-type reflections, whereas these reflections were relatively intense in the same specimens when they were annealed. On the other hand, annealing did not appear to affect other regions of the system as dramatically. The diagram presented in Fig. 1 is based upon results obtained from annealed specimens.

Solid solution regions prevail at both ends of the system. The solubility of NdBr<sub>3</sub> in TbCl<sub>3</sub> is modest compared to that of TbCl<sub>3</sub> in NdBr<sub>3</sub>. The former exhibits only a  $\sim 12.5$  mole% solubility range; the latter exhibits a 47.5 mole% solubility range. The low solubility of NdBr<sub>3</sub> in TbCl<sub>3</sub> is reminiscent of that observed in the NdCl<sub>3</sub>–NdBr<sub>3</sub> ternary system (1) in which a PuBr<sub>3</sub>-type structure prevailed only over a  $\sim 5$  mole% range; the UCl<sub>3</sub>-type structure which is common to NdCl<sub>3</sub> then appeared. The appearance of the UCl<sub>3</sub>-type structure in this work at a relatively low mole percentage substitution limit provides insight into the atomic distribution as is discussed below.

For the most part the system behavior can be interpreted from radius ratio considerations, where radius ratio is defined as R=  $r(X^{-})/r(M^{3+})$ , even though quantitative radius ratio calculations are not meaningful for mixed systems such as these. In both the  $LnCl_3$  and  $LnBr_3$  systems one observes the following structure types with increasing R: UCl<sub>3</sub>-, PuBr<sub>3</sub>- (which for  $LnCl_3$  prevails over a relatively narrow R region), AlCl<sub>3</sub>- (which for  $LnBr_3$  is stable over a very narrow R region), and finally the FeCl<sub>3</sub>-type structure (3, 15). R for NdBr<sub>3</sub> and TbCl<sub>3</sub> are reported in (18) as 1.960 and 1.961, respectively; they are 1.45 and 1.41, respectively, based on Shannon's radii (5).

In this system as NdBr<sub>3</sub> is added to pure TbCl<sub>3</sub> the Nd<sup>3+</sup> and Br<sup>-</sup> ions substitute into the TbCl<sub>3</sub> lattice and the radius ratio as it pertains to any particular cation can effectively either be increased or decreased, depending upon the distribution of anions around that cation. If solid solution with a random atomic distribution continued to prevail, the PuBr<sub>3</sub>-type structure should persist. However, the UCl<sub>3</sub>-type structure appears. This unexpected appearance is indicative of some level of cation and anion ordering, or preference, i.e., Cl<sup>-</sup> anions must preferentially coordinate Nd<sup>3+</sup> cations and Br<sup>-</sup> anions must preferentially coordinate Tb<sup>3+</sup> cations, as is discussed later.

The opposite (high NdBr<sub>3</sub> mole%) end of

the system exhibits an extended PuBr<sub>3</sub>-type solubility region that bears little resemblance to the behavior observed in the ternary Tb-Cl-Br system (3), apparently because extensive cation substitution (Nd<sup>3+</sup> for Tb<sup>3+</sup>) has occurred and changed the effective Ln<sup>3+</sup> radius. In the ternary Tb-Cl-Br system the PuBr<sub>3</sub>-type structure prevailed only to the  $\sim 15$  mole% tribromide composition while in the ternary Gd-Cl-Br system this structure prevailed over a 25 mole% range, from 20 to 45 mole% tribromide. The present behavior is reflective of the PuBr<sub>3</sub>-type solubility regions exhibited by both of these systems. With an effective cation radius larger than that of Tb<sup>3+</sup> (because of the presence of  $Nd^{3+}$ ) which increases as the NdBr<sub>3</sub> content is increased, the R range over which the PuBr<sub>3</sub>type structure retains stability appears extended and approximates that of both the Tb-Cl-Br and Gd-Cl-Br systems. Again, as TbCl<sub>3</sub> is added to NdBr<sub>3</sub> and by analogy to the Gd-Cl-Br ternary system (3),  $Cl^{-}$ anions selectively coordinate the larger Nd<sup>3+</sup> and favor UCl<sub>3</sub>-type structure formation. It is consequently the first phase that appears near the end of the NdBr<sub>3</sub> extended solid solution region (from 52.5 to 100 mole% NdBr<sub>3</sub>, or from 0 to 47.5 mole% TbCl<sub>3</sub>). Ion segregation of Cl<sup>-</sup> anions in the UCl<sub>3</sub>-type phase causes an AlCl<sub>3</sub>-type phase to appear soon thereafter with concomitant disappearance of the PuBr<sub>3</sub>-type structure.

It is helpful to think of the entire system in terms of changing R values. If one imagines starting with pure TbCl<sub>3</sub> and substituting Nd<sup>3+</sup> for Tb<sup>3+</sup> and Br<sup>-</sup> for Cl<sup>-</sup> only the common PuBr<sub>3</sub>-type structure persists to the solubility limit discussed previously, ~5 mole%. Beyond this solubility limit a significant cation and anion reordering occurs. The appearance of the UCl<sub>3</sub>-type Nd (Cl,Br)<sub>3</sub> phase (found with small R values) indicates that the Cl<sup>-</sup> ions have combined predominantly with the Nd<sup>3+</sup> cations, and the Br<sup>-</sup> anions with the Tb<sup>3+</sup> cations. The molar volume of the UCl<sub>3</sub>-type structure at the 10 mole% NdBr<sub>3</sub> composition, the minimum composition for which parameters could be determined, is 195.2 Å<sup>3</sup>, and is very close to that of pure NdCl<sub>3</sub> (200.4 Å<sup>3</sup>). This UCl<sub>3</sub>-type phase persists to the 60 mole% NdBr<sub>3</sub> composition; in the ternary Nd-Cl-Br system the UCl<sub>3</sub>-type structure prevails to 70 mole% tribromide. This small difference is presumed to result because the limited cation miscibility has effectively altered slightly the cation radius.

At ~12.5 mole% NdBr<sub>3</sub>, as a result of Cl<sup>-</sup> ions combining preferentially with Nd<sup>3+</sup> cations in the UCl<sub>2</sub>-type phase, the effective size of those anions associated with  $Tb^{3+}$  has increased such that the PuBr<sub>3</sub>-type structure can no longer be sustained. The structure type common for larger R values, the AlCl<sub>3</sub>-type structure, which spans the range  $\sim 1.993 < R < \sim 2.079$  (18), and the UCl<sub>3</sub>-type region, which spans the radius ratio range  $\sim 1.706 < R < \sim 1.930$  (18), then prevail. As the NdBr<sub>3</sub> content is increased, the ions are distributed preferentially between the UCl<sub>3</sub>- and AlCl<sub>3</sub>-type phases, and the radius ratio values associated with each of these phases slowly converge. At 50 mole% NdBr<sub>3</sub> the AlCl<sub>3</sub>-type phase disappears and at 52.5 mole% NdBr<sub>3</sub> local R values are such that the PuBr<sub>3</sub>-type phase reappears. The UCl<sub>3</sub>-type (predominantly) Nd(Cl,Br)<sub>3</sub> material by now has become adequately Br<sup>-</sup>-rich so that it too converts to the PuBr<sub>3</sub>-type structure; this structure type prevails thereafter.

Although the behavior of this mixed system and the phases observed can be understood on the basis of radius ratio considerations, the presence of the UCl<sub>3</sub>-type structure which exists over an effective radius ratio range *smaller* than that of either pure phase was not expected. Only a nonrandom cation/anion arrangement could create effective radii that would allow this structure-type field of stability to persist over such an extended range. The nine-coordinate UCl<sub>3</sub>-type structure is exhibited by  $LnCl_3$  species for Ln = La-Gd. Thus Nd is near the middle of this field of stability. Presumably the greater stabilization which results from the higher coordination provided by Cl<sup>-</sup> anions supplies the driving force that selectively concentrates Cl<sup>-</sup> anions in this phase. On the other hand, TbBr<sub>3</sub> is near the interface of the six-coordinateeight-coordinate stability region. The Tb<sup>3+</sup> ion by combining preferentially with Br<sup>-</sup> anions not only achieves more optimum coordination stability, but also contributes to the driving force needed to separate the anions.

Observation of a quenchable high-temperature modification that disappeared upon annealing and the differing phase limits observed in the 7.5–17.5 mole% NdBr<sub>3</sub> region with annealing demonstrate the phase limit dependence upon thermal treatment. Under different thermal conditions slightly different phase limits might be observed.

#### Acknowledgment

Support of the National Science Foundation, Division of Materials Research, Solid State Chemistry Program, DMR 84-00739, is acknowledged gratefully.

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